

- VI. A salesperson must visit 4 of 6 stores and order is important. That is, AB and BA represent different routes. How many routes are available to the salesperson?

$${}_N P_R = \frac{N!}{(N-R)!}$$

$${}_6 P_4 = \frac{6!}{(6-4)!} = \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{2 \times 1} = 6 \times 5 \times 4 \times 3 = 360$$

- VII. Redo problem VI assuming order does not count. AB and BA are the same and count as one route. Be sure to use a formula and show all work.

$${}_N C_R = \frac{N!}{(N-R)!(R!)}$$

$${}_6 C_4 = \frac{6!}{(6-4)!4!} = \frac{6 \times 5 \times 4 \times 3 \times 2 \times 1}{2 \times 1 \times 4 \times 3 \times 2 \times 1} = \frac{6 \times 5}{2 \times 1} = 15$$

- VIII. How many different 3-person subcommittees can be chosen from an 8-person committee?

$${}_N C_R = \frac{N!}{(N-R)!(R!)}$$

$${}_8 C_3 = \frac{8!}{(8-3)!3!} = \frac{8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{5 \times 4 \times 3 \times 2 \times 1 \times 3 \times 2 \times 1} = 8 \times 7 = 56$$

- IX. Three of 8 committee members must be chosen to give a speech. All 8 have very different personalities and order is important. How many different speaker arrangements are possible?

$${}_N P_R = \frac{N!}{(N-R)!}$$

$${}_8 P_3 = \frac{8!}{(8-3)!} = \frac{8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{5 \times 4 \times 3 \times 2 \times 1} = 8 \times 7 \times 6 = 336$$

- X. How many 4-place random numbers can be generated from 10 digits? Repeating digits is allowed.

This is a special adaptation of the counting rule because with each choice you have 10 digits to choose from.

$$\text{MNOP where all equal 10 is } 10 \times 10 \times 10 \times 10 = 10^4 = 10,000$$

- XI. Six parts are to be inspected from a production process designed to have approximately 5% defective parts. Using the binomial formula, determine the probability of zero defects. Use a table to determine the probability of at least 2 defective parts. State the entire probability distribution. What is the probability of 2 defective parts?

- A. The Poisson approximation of the binomial can not be used because n is not  $\geq 30$ .

$$P(x) = \frac{n!}{x!(n-x)!} p^x q^{n-x}$$

$$P(0) = \frac{6!}{0!(6-0)!} .05^0 .95^{6-0} = \frac{1}{1}(1) .95^6 = .7351 = 73.51\%$$

- B.

$$P(x \geq 2) = 1 - [P(0) + P(1)] = 1 - (.735 + .232) = 1 - .967 = .033 = 3.3\%$$

- C. See page ST 1 for the entire distribution.

D.  $P(x=2) = .031$

- XII. Approximately 4% of the estimated 100 travelers driving on route 128 will stop for a snack between 11:10 PM and 11:20 PM. Is the Poisson approximation to the binomial distribution appropriate for the solution of this problem? Use a table to determine the probability that less than 2 travelers will stop for a snack. Draw a graph of this distribution.

A Poisson approximation of the binomial is appropriate.

$$n \geq 30 \text{ as } n = 100$$

$$np < 5 \text{ as } np = .04 \times 100 = 4$$

$$\mu = np = (100)(.04) = 4$$

$$P(< 2) = P(0) + P(1) = .0183 + .0733 = .0916 = 9.16\%$$

