

IV. Linda Smith is using ANOVA to measure whether there is a difference between the average weekly sales of her 3 salespeople. The test will be at the .05 level of significance.

A. These are the null hypothesis and alternate hypothesis.

$$H_0 : \mu_1 = \mu_2 = \mu_3 \quad H_1 : \mu_1 \neq \mu_2 \neq \mu_3$$

B. The level of significance for this single treatment, one-tail problem will be .05.

C. F is the test statistic.

$$F = \frac{\text{Estimated variance between the treatments}}{\text{Estimated variance within the treatments}}$$

**Note:** Salespeople is the treatment variable and sales is the response variable.

Variance Analysis Summary Table				
Variance Sources	df	Sum of the Squares	Mean Squares (variance)	ANOVA
Between Treatments	t - 1	SS <sub>T</sub>	MS <sub>T</sub> = $\frac{SS_T}{t-1}$	F = $\frac{MS_T}{MS_E}$
Within Treatments (error)	N - t	SS <sub>E</sub>	MS <sub>E</sub> = $\frac{SS_E}{N-t}$	
Total Variance	N - 1	SS <sub>TOTAL</sub>		

t is the number of treatments

n is the number of rows in a treatment

N is total observations

SS<sub>T</sub> is the sum of the squares for treatments

SS<sub>E</sub> is the sum of the squares for error

SS<sub>TOTAL</sub> is the total sum of the squares

MS<sub>T</sub> is the mean squares for treatments

MS<sub>E</sub> is the mean squares for error

D. Reject the null hypothesis when F from the test statistic is beyond the critical value of F for the .05 level of significance.

E. Apply the decision rule.

df = t - 1 = 3 - 1 = 2 for the numerator  
df = N - t = 12 - 3 = 9 for the denominator  
F's critical value is 4.26.

Weekly Sales (x) in Thousands of Dollars for 3 Treatments (T)						Row Totals Required for Calculations
	Salesperson L is T <sub>1</sub>		Salesperson M is T <sub>2</sub>		Salesperson N is T <sub>3</sub>	
	Sales (X <sub>1</sub> )	X <sub>1</sub> <sup>2</sup>	Sales (X <sub>2</sub> )	X <sub>2</sub> <sup>2</sup>	Sales (X <sub>3</sub> )	X <sub>3</sub> <sup>2</sup>
	7	49	6	36	9	81
Column Totals	6	36	8	64	8	64
Required for	7	49	6	36	7	49
Calculations	4	16	6	36	10	100
Σ X <sub>T</sub>	24		26		34	
(Σ X <sub>T</sub> ) <sup>2</sup>	576		676		1156	
n	4		4		4	
$\frac{(\sum X_T)^2}{n}$	144		169		289	
Σ X <sub>T</sub> <sup>2</sup>		150		172		294

$$SS_T = \sum \left[ \frac{(\sum X_T)^2}{n} \right] - \frac{(\sum X)^2}{N}$$

$$= 602 - \frac{84^2}{12}$$

$$= 602 - 588 = 14$$

$$SS_E = \sum X^2 - \sum \left[ \frac{(\sum X_T)^2}{n} \right]$$

$$= 616 - 602$$

$$= 14$$

Total variance equals SS<sub>T</sub> + SS<sub>E</sub> = 14 + 14 = 28. Total variance also equals

$$SS_{TOTAL} = \sum X^2 - \frac{(\sum X)^2}{N}$$

$$= 616 - 588 = 28$$

**Note:** Half the variability has been explained by the treatment variable.

$$MS_T = \frac{SS_T}{t-1} = \frac{14}{3-1} = 7.0$$

$$MS_E = \frac{SS_E}{N-t} = \frac{14}{12-3} = \frac{14}{9} = 1.56$$

Reject H<sub>0</sub> because F =  $\frac{MS_T}{MS_E} = \frac{7.0}{1.56} = 4.49$  and 4.49 > 4.26. Mean sales of these salespeople are not equal.